

075 & 076 Log and exponential – differentiation and integration

Exponential functions:

| | With chain rule: | Integral: |
|---|---|---|
| $y = e^x$ $\frac{dy}{dx} = e^x$ | $y = e^u$ $\frac{dy}{dx} = e^u \frac{du}{dx}$ | $\int e^x dx = e^x + C$ |
| $y = a^x$ $\frac{dy}{dx} = (\ln a)a^x$ | $y = a^u$ $\frac{dy}{dx} = (\ln a)a^u \frac{du}{dx}$ | $\int a^x dx = \frac{1}{\ln a} a^x + C$ |

Log functions:

| | With chain rule: | Integral: |
|---|---|--|
| $y = \ln x$ $\frac{dy}{dx} = \frac{1}{x}$ | $y = \ln f(x)$ $\frac{dy}{dx} = \frac{f'(x)}{f(x)}$ | $\int \frac{1}{x} dx = \ln x + C$ $\int \frac{f'(x)}{f(x)} dx = \ln f(x) + C$ |
| $y = \log_b x$ $\frac{dy}{dx} = \frac{1}{\ln b} \frac{1}{x}$ | $y = \log_b f(x)$ $\frac{dy}{dx} = \frac{1}{\ln b} \frac{f'(x)}{f(x)}$ | |